

# Measurements of Jet and Multijet Cross Sections with the CDF Detector

Matthias Tönnesmann

Max-Planck-Institut für Physik, Munich  
Michigan State University

[matthias@mppmu.mpg.de](mailto:matthias@mppmu.mpg.de)

(On behalf of the CDF collaboration)

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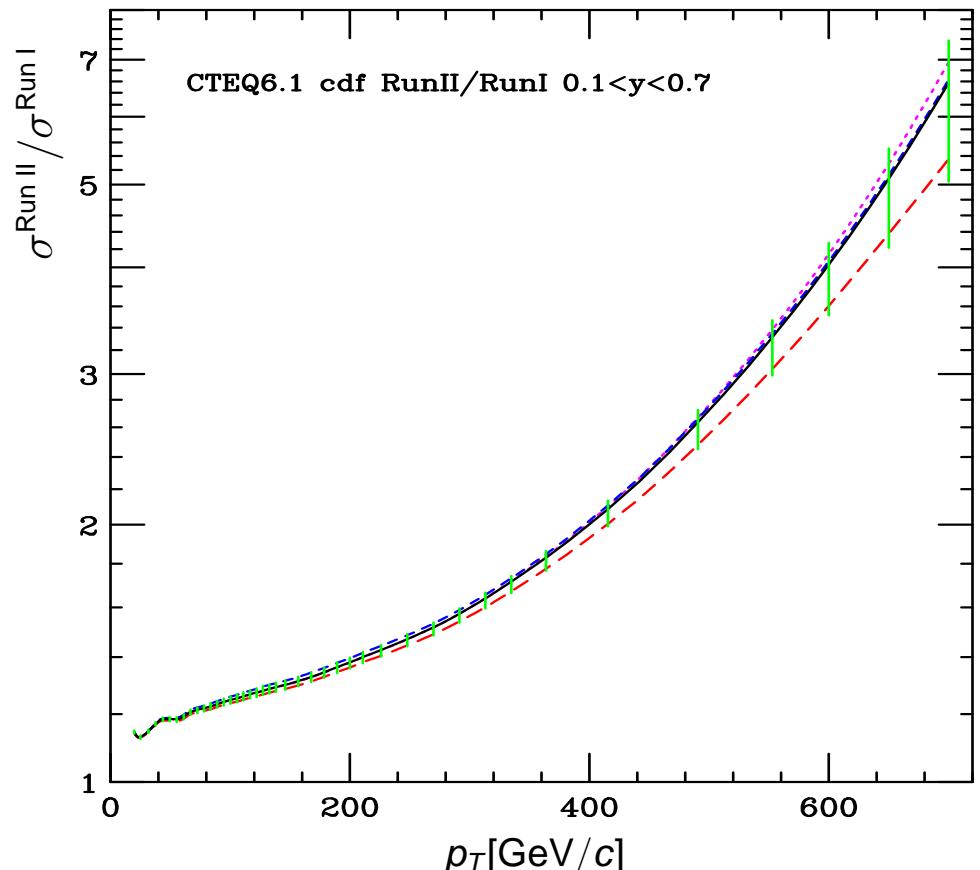
18 July 2003

- Outline:**
1. Run II Inclusive Jet Cross Section
    - Status
    - Prospects
  2. Run I Inclusive 3-Jet Cross Section vs. NLO QCD



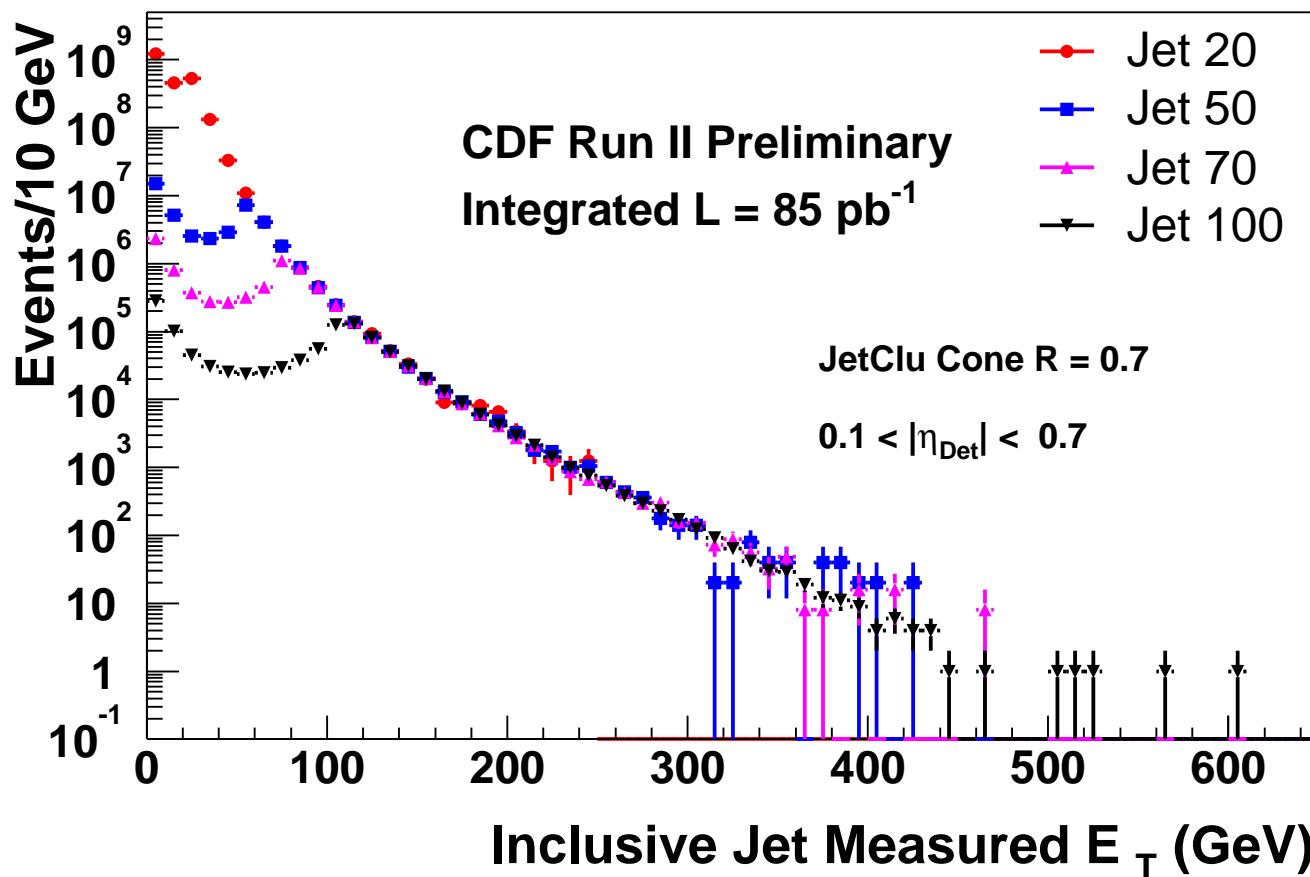
# Inclusive Jet Cross Section — Motivation

- Measure fundamental input ingredients of QCD:
  - parton distribution functions: Excess at high  $E_T$  in CDF Run I data.  
Gluon distribution not constrained at high  $x$ .  
CTEQ 6.1: Good agreement with Run I data within uncertainty.
  - strong coupling constant  $\alpha_s$
- Probe small distances and look for deviations from QCD predictions. (New physics?)
- Extend measured  $E_T$  spectrum to  $> 600 \text{ GeV}$ :
  - integrated luminosity goal (Run IIa):  $2 \text{ fb}^{-1}$ .
  - higher  $\sqrt{s}$ :  $1.8 \rightarrow 1.96 \text{ TeV}$ :  
cross section  $\times 2$  @  $E_T = 400 \text{ GeV}$   
 $\times 4$  @  $E_T = 600 \text{ GeV}$
- Run II so far:
  - Feb. 2002 - Jan. 2003:  $\mathcal{L}_{\text{int}} = 85 \text{ pb}^{-1}$   
→ corrected cross section:  
Repeat Run I analysis (fixed cone jet algorithm **JetClu**,  $R_{\text{cone}} = 0.7$ ;  
Run I corrections).
  - Feb. 2002 - July 2003:  $\mathcal{L}_{\text{int}} = 146 \text{ pb}^{-1}$   
→ raw distributions



# Inclusive Jet Cross Section — Event selection

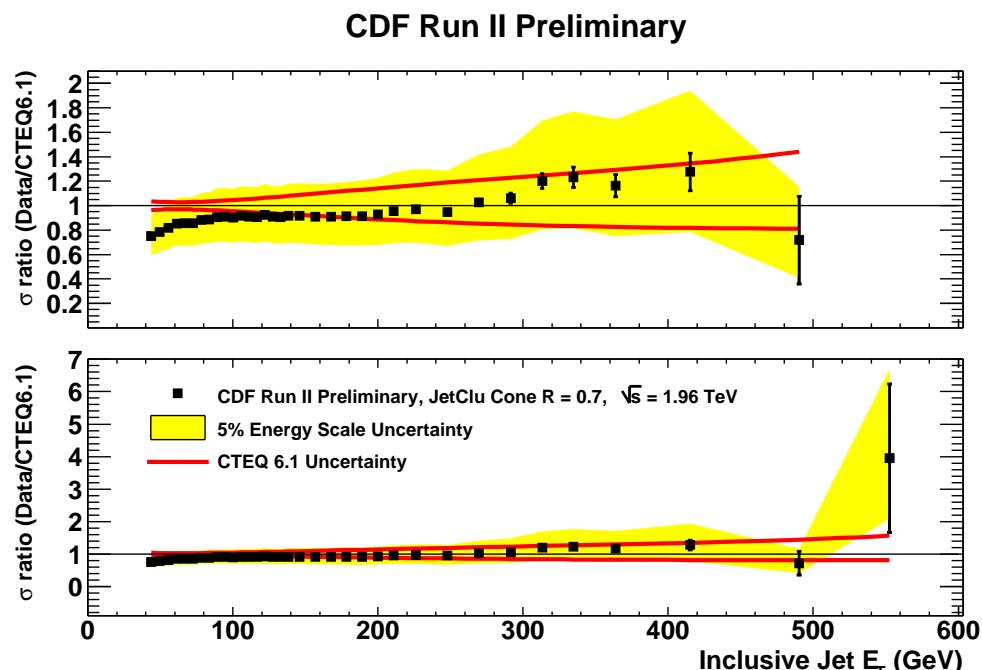
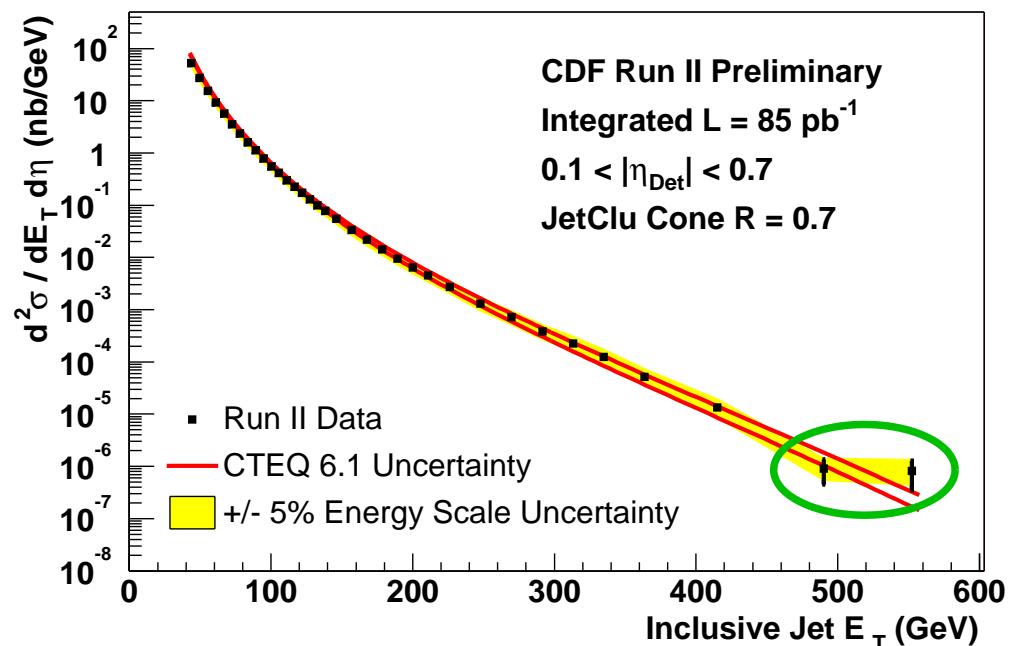
- 4 Triggers: Jet20, Jet50, Jet70, Jet100. Use where  $> 99\%$  efficient.
- $E_T/\sqrt{\sum E_T} < 3.5 \dots 7 \sqrt{\text{GeV}}$ .
- $|z_{\text{vertex}}| < 60 \text{ cm}$ .
- $\sum E_T < 1500 \text{ GeV}$ .
- Raw distributions ( $0.1 < |\eta_{\text{Det}}| < 0.7$ ):



# Inclusive Jet Cross Section — Corrections and Results

- Correct jet energies back to hadron level.
- Calorimeter energy scale set to Run I scale.
  - Apply  $(5 \pm 5)\%$  correction to raw energy.
  - **largest source of systematic uncertainty.**
- Apply Run I corrections for:
  - calorimeter non-linearity
  - smearing due to resolution
  - underlying event and multiple interactions

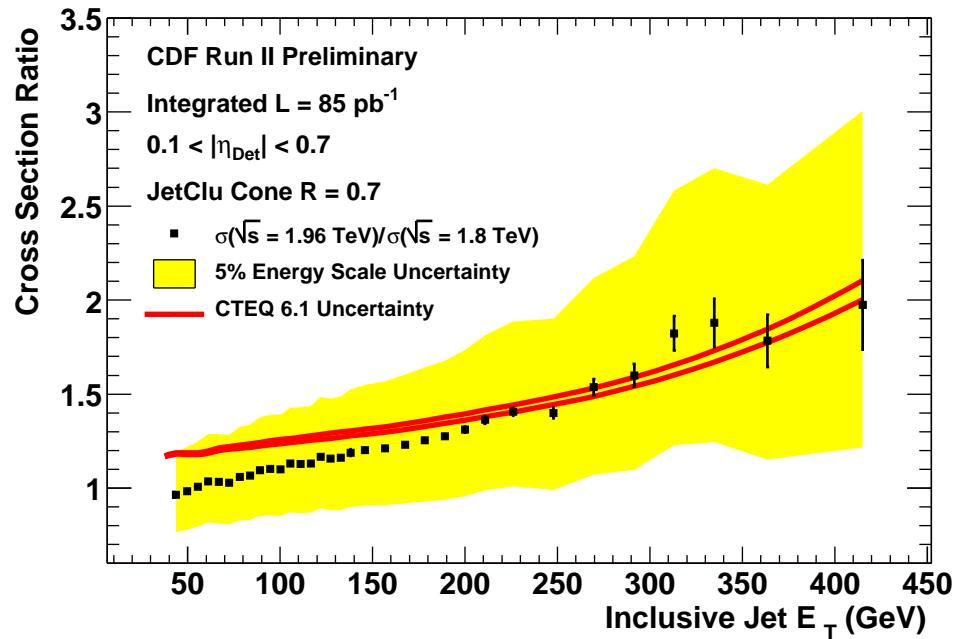
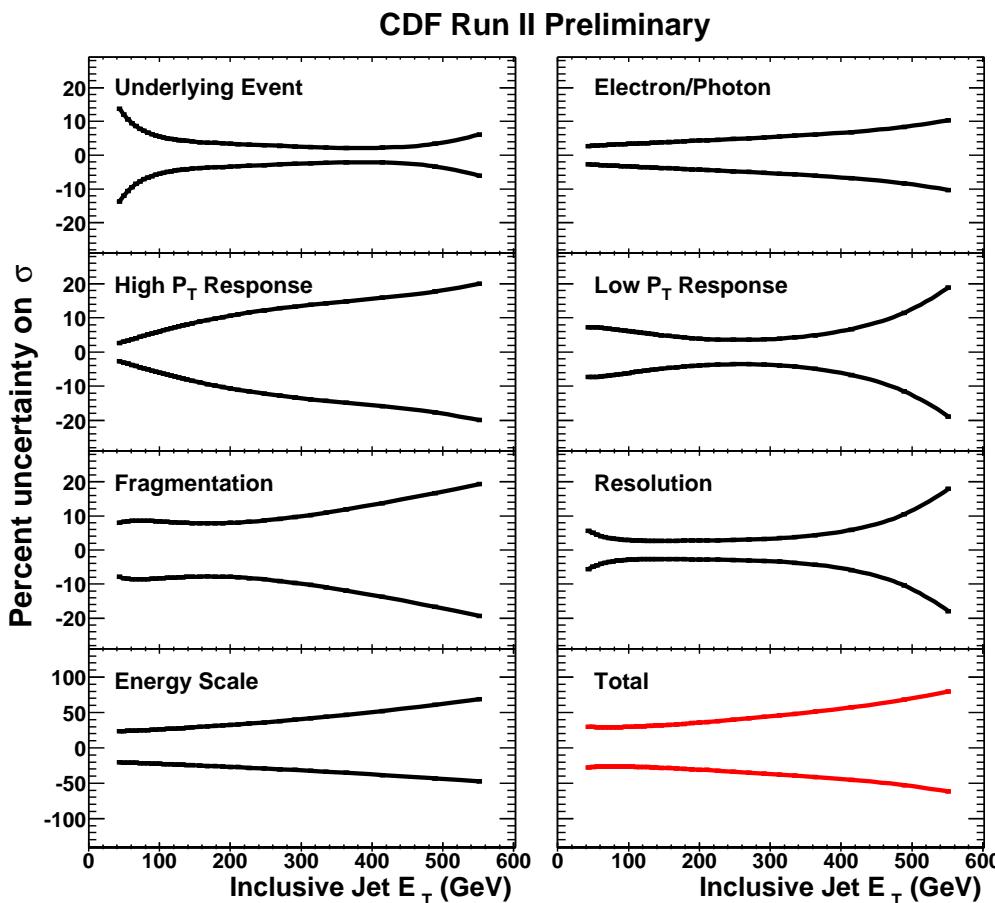
- Two data points added w.r.t. Run I.  
 $E_T$  range extended by 150 GeV.
- Measured cross section agrees with prediction within uncertainties.
- Largest upward deviation in CTEQ 6.1 band:  
**increased gluon content at high  $x$ .**



# Inclusive Jet Cross Section — Run II vs. Run I and Systematics

## Comparison with Run I

- $\sigma^{\text{Run II}}/\sigma^{\text{Run I}}$ : Systematic errors mostly cancel, but Run II jet energy scale is dominant.
- Reasonable agreement, but more work needed to understand the details.
- $\times 2$  @  $E_T = 400 \text{ GeV}$  confirmed.

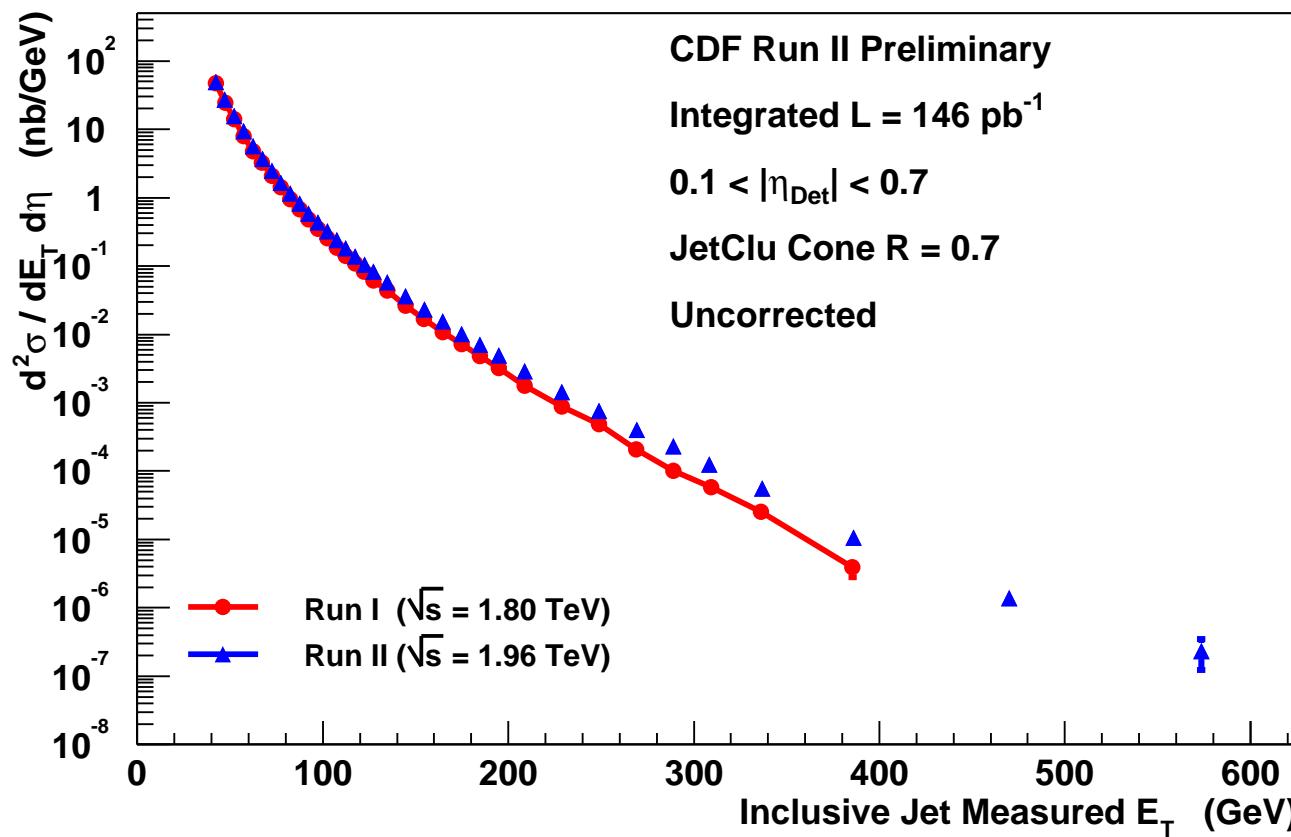


## Systematic uncertainties

- dominant source: energy scale (under study).
- luminosity:  $\pm 5.8 \%$ .

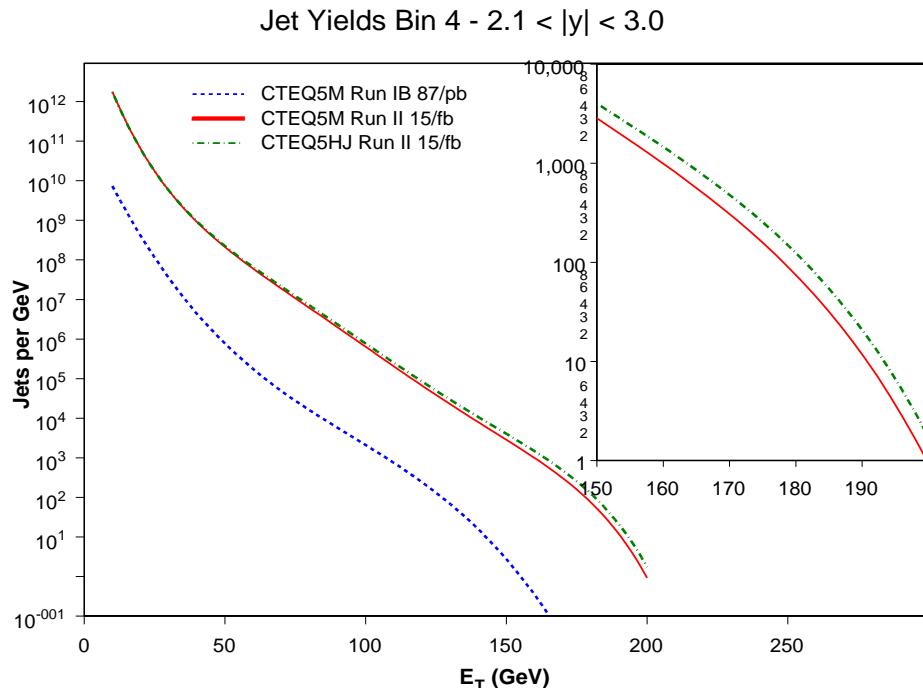
# Inclusive Jet Cross Section — Next Steps

- Better understanding of calorimeter response. → Reduce systematic uncertainty.
- Collect more data. → Reduce statistical uncertainty.
- $\mathcal{L}_{\text{int}} = 146 \text{ pb}^{-1}$ :



# Inclusive Jet Cross Section — Forward Region

- New CDF plug calorimeter:  $1.1 < |\eta_{\text{Det}}| < 3.6$ .

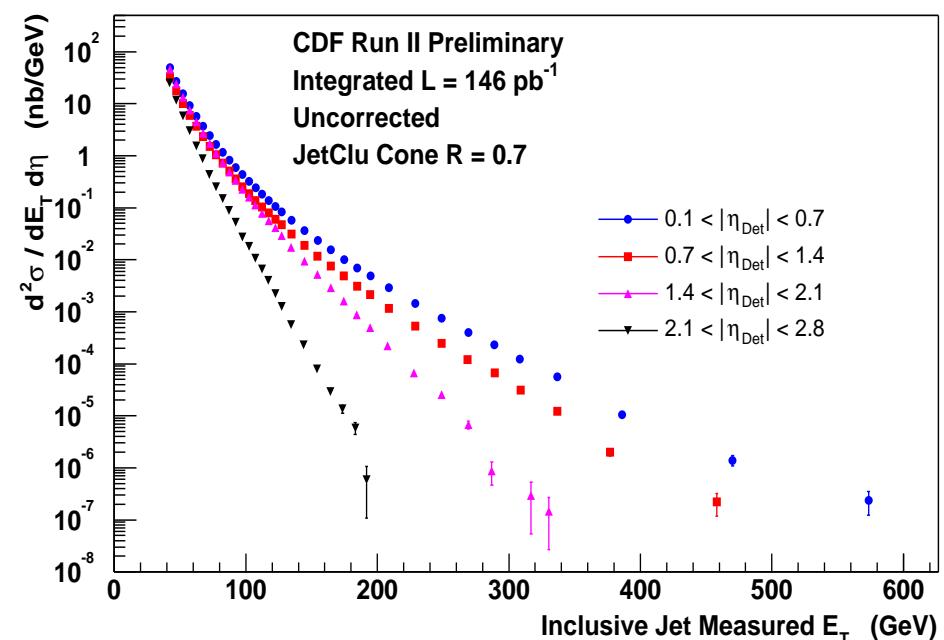


Theory:

- Sensitivity to high  $x$  gluon at high rapidities.
- Constraint on parton distribution functions.

CDF measurement:

- Only raw distributions so far.
- To be done: Study calorimeter response (calibration, jet energy scale  $\rightarrow$  response function) and systematic uncertainties in the forward region.



# Inclusive Jet Cross Section — KtClus algorithm

- KtClus combines particles based on relative transverse momentum:

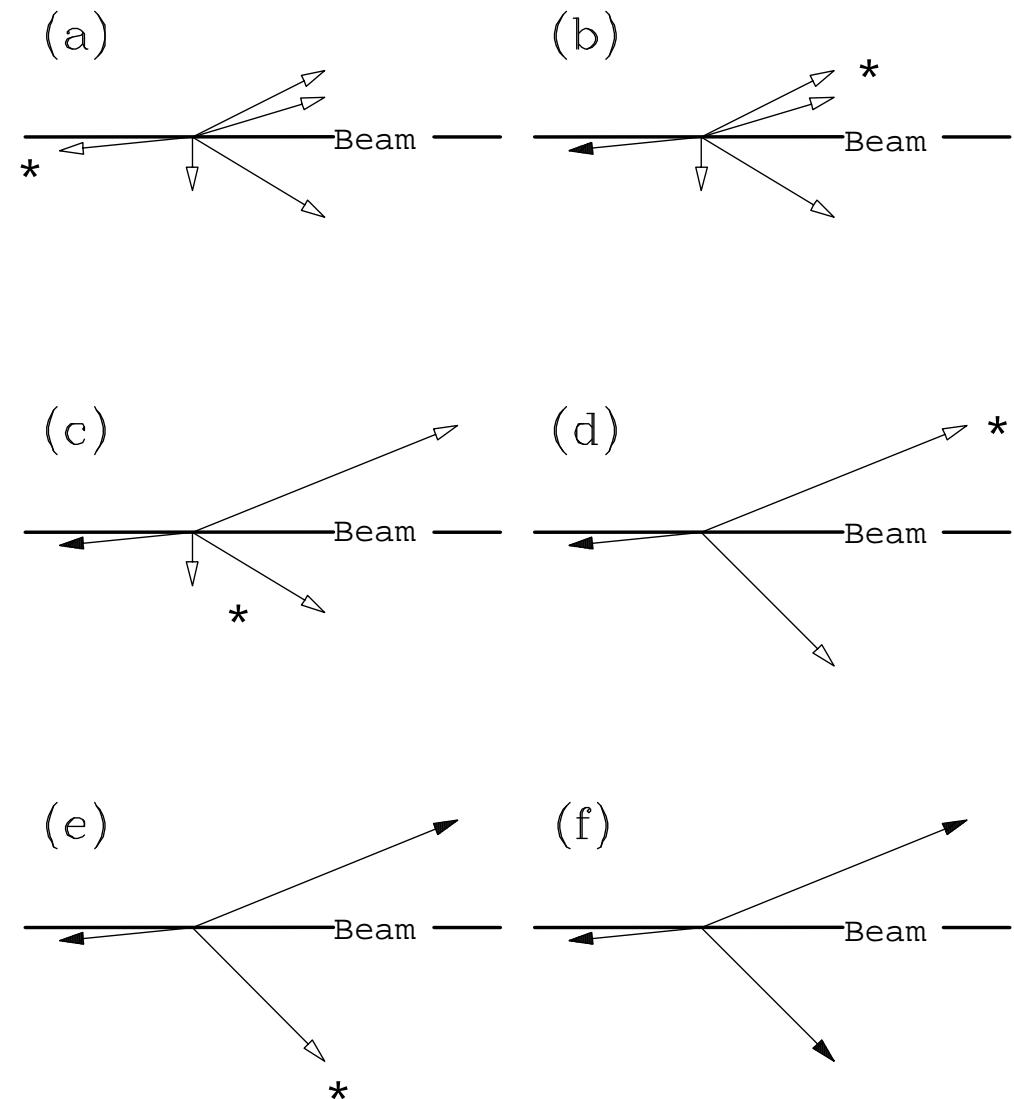
$$d_{ij} = \frac{\min(E_{T,i}^2, E_{T,j}^2) \cdot (\Delta R)^2}{D^2}, \quad d_i = E_{T,i}^2.$$

$\min(d_{ij}, d_i) = d_{ij}$  → merge  $i$  and  $j$ .

$\min(d_{ij}, d_i) = d_i$  → promote  $i$  to a jet.

$D$  controls the size of the jets.

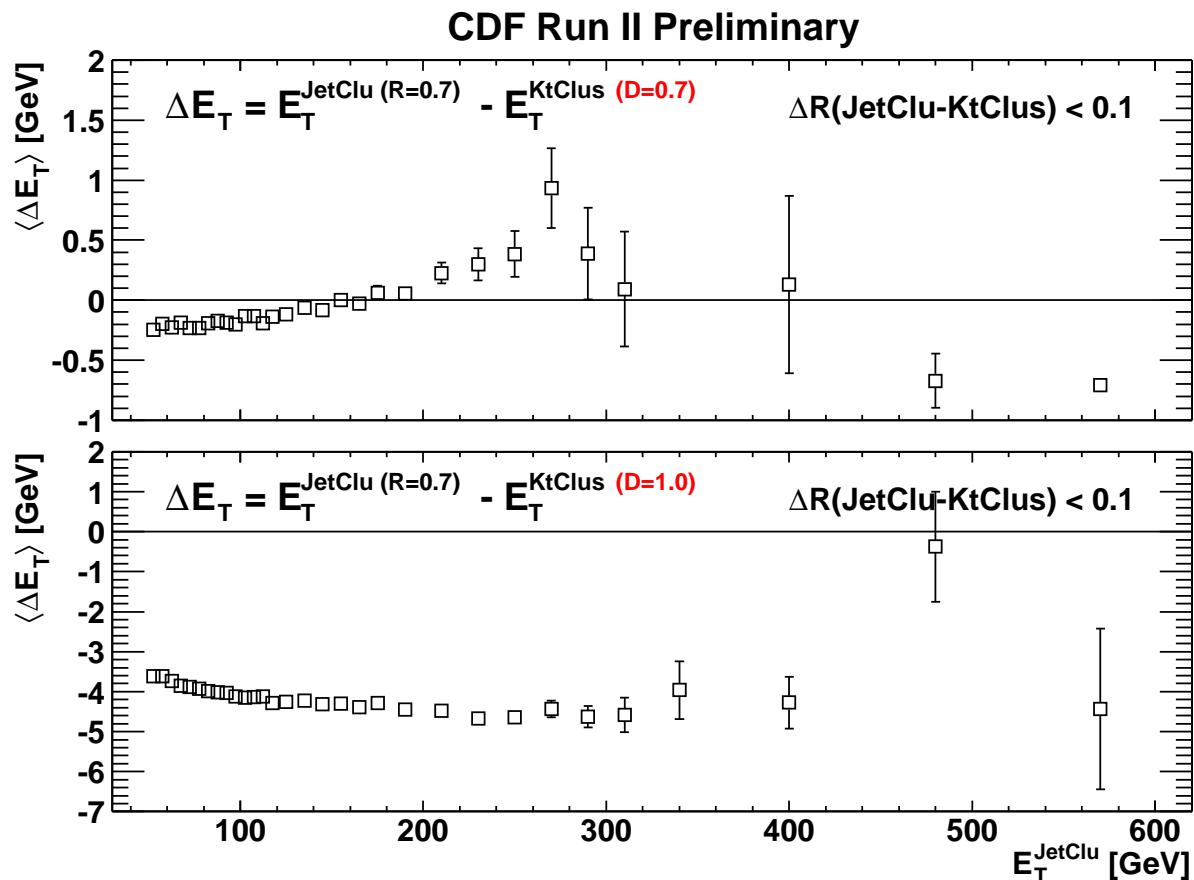
- No splitting/merging prescription required.
- Infrared and collinear safe.
- Theoretically preferred (and used by DØ):  
 $D = 1.0$ .
- Compare JetClu ( $R_{\text{cone}} = 0.7$ ) to  
KtClus ( $D = 0.7, D = 1.0$ ).



# Inclusive Jet Cross Section — $E_T$ : JetClu vs. KtClus

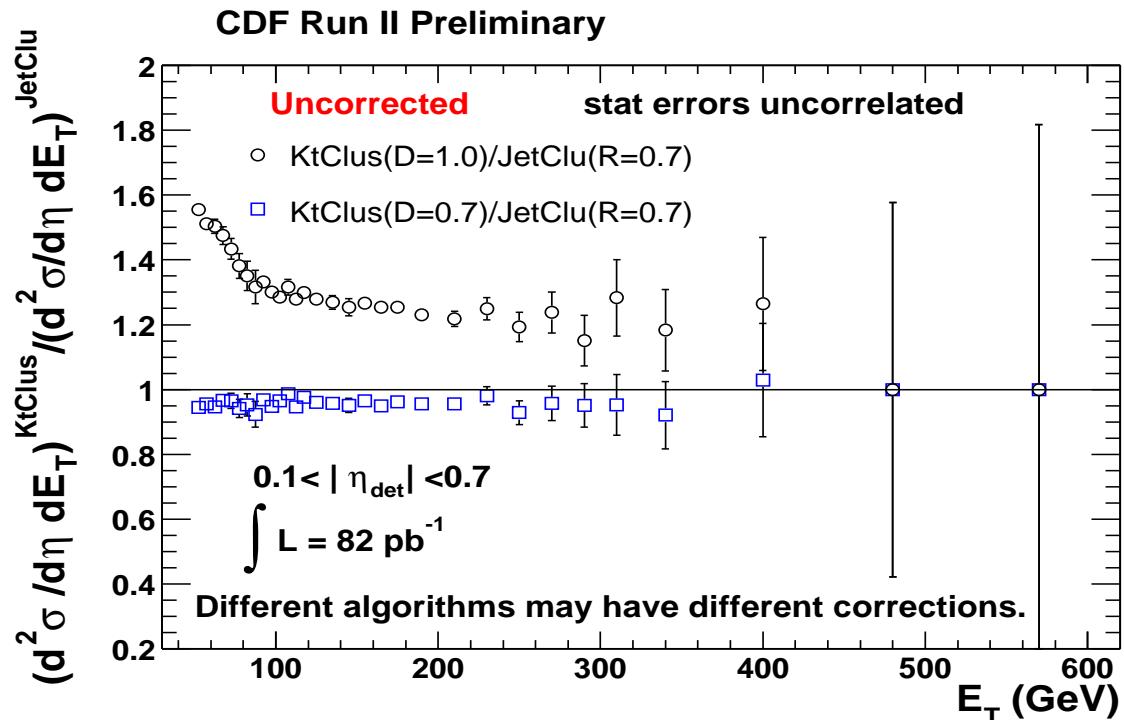
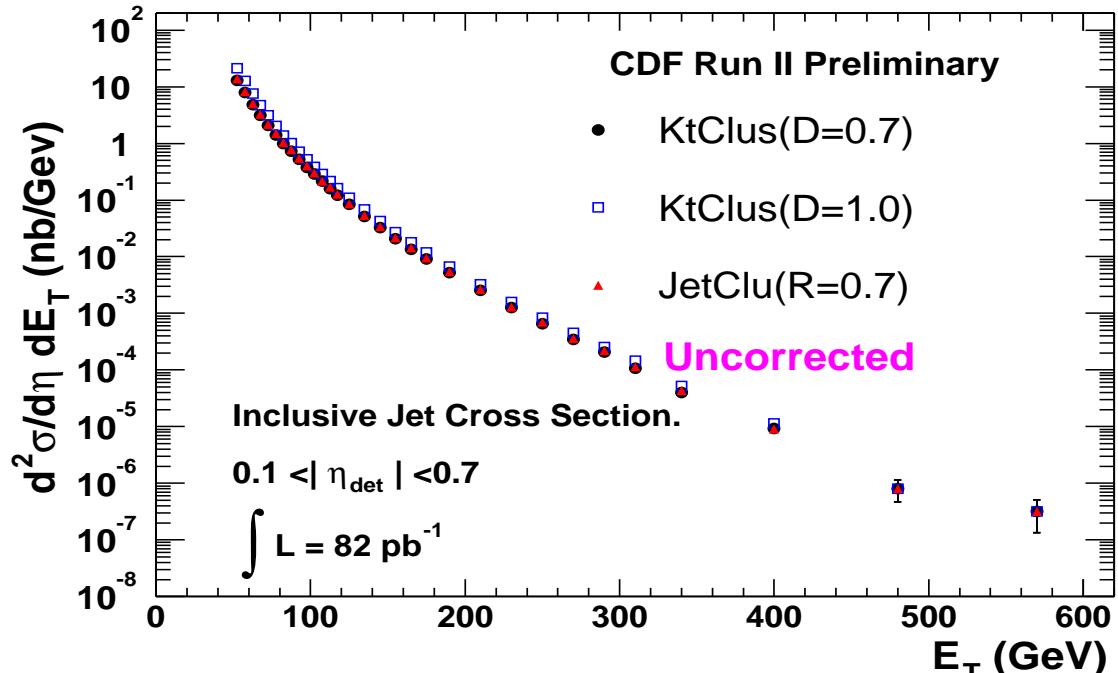
- Compare  $E_T$  of JetClu and matched KtClus jets:
  - Choose JetClu jet.
  - Find corresponding KtClus jet. Matching requirement:  $\Delta R < 0.1$ .
  - Plot mean  $\Delta E_T$ (JetClu-KtClus) vs.  $E_T$ (JetClu).
- Dataset:  $\mathcal{L}_{\text{int}} = 82 \text{ pb}^{-1}$  of CDF Run II data.
- Event selection:  $\widetilde{E}_T < 6 \sqrt{\text{GeV}}$ ,  $\sum E_T < 1960 \text{ GeV}$ ,  $|Z_{\text{vertex}}| < 60 \text{ cm}$ .

- $D = 0.7$ : Small differences to JetClu ( $R_{\text{cone}} = 0.7$ ). Non-constant shift.
- $D = 1.0$ : Up to 4-5 GeV higher  $E_T$  in KtClus jets.
- Cannot apply JetClu jet energy corrections to KtClus jets.



# Inclusive Jet Cross Section — $\sigma^{\text{raw}}$ : JetClu vs. KtClus

- Large differences between  $D = 0.7$  and  $D = 1.0$ .
- Shape at low  $E_T$  different.
- **Caveat:** These are **uncorrected** distributions.
- **Long** term goal: Measure jet cross section using the Run II jet algorithms (**KtClus**, **MidPoint**):
  - Derive jet energy corrections.
  - Study jet fragmentation.
  - Study energy contributions from underlying event.
  - ...



# 3-Jet Production vs. NLO QCD

- Full NLO QCD prediction for 3-jet production at hadron colliders by Kilgore & Giele: hep-ph/0009193.

→ allow for a measurement of  $\alpha_s$  from  $R_{32} = \frac{\sigma^{3\text{-jet}}}{\sigma^{2\text{-jet}}}$   
or from event shapes.

- Comparison to Run Ib data.
- Event selection:

- Jet reconstruction using JetClu,  $R_{\text{cone}} = 0.7$ .
- Trigger:  $\sum E_T > 175 \text{ GeV}$ .
- Require  $\geq 3$  jets with  $E_T > 20 \text{ GeV}$ ,  $|\eta| < 2.0$ .  
 $\sum E_T^{\text{3 jets}} > 320 \text{ GeV}$ .

Cone separation:  $\Delta R > 1.0$ .

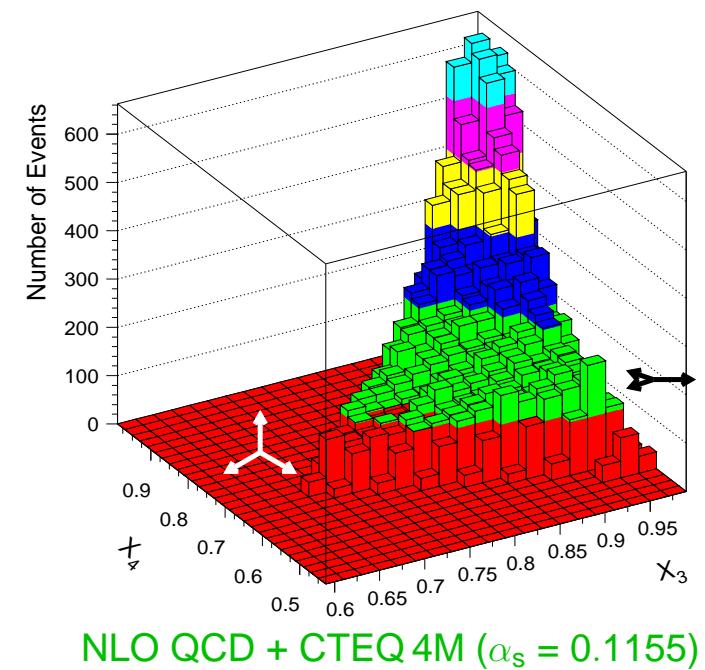
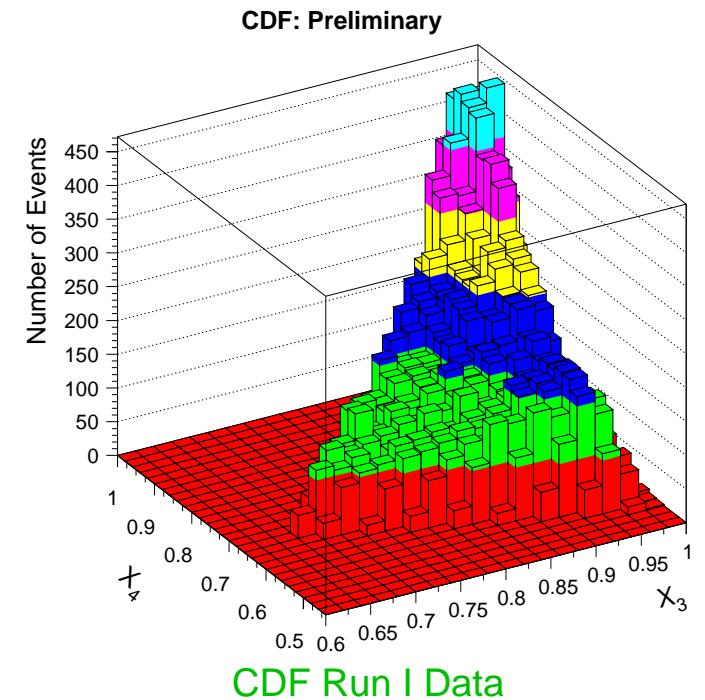
(Reduces  $s_{\min}$  dependence in NLO QCD prediction.)

- Remove and correct for multiple interactions.
- Boost into 3-jet rest frame. Number 3 leading jets such that:  
 $E_3 > E_4 > E_5$  ( $1 + 2 \rightarrow 3 + 4 + 5$ ).

- Dalitz variables  $X_i = \frac{2 E_i}{m_{\text{3 jets}}}$ :

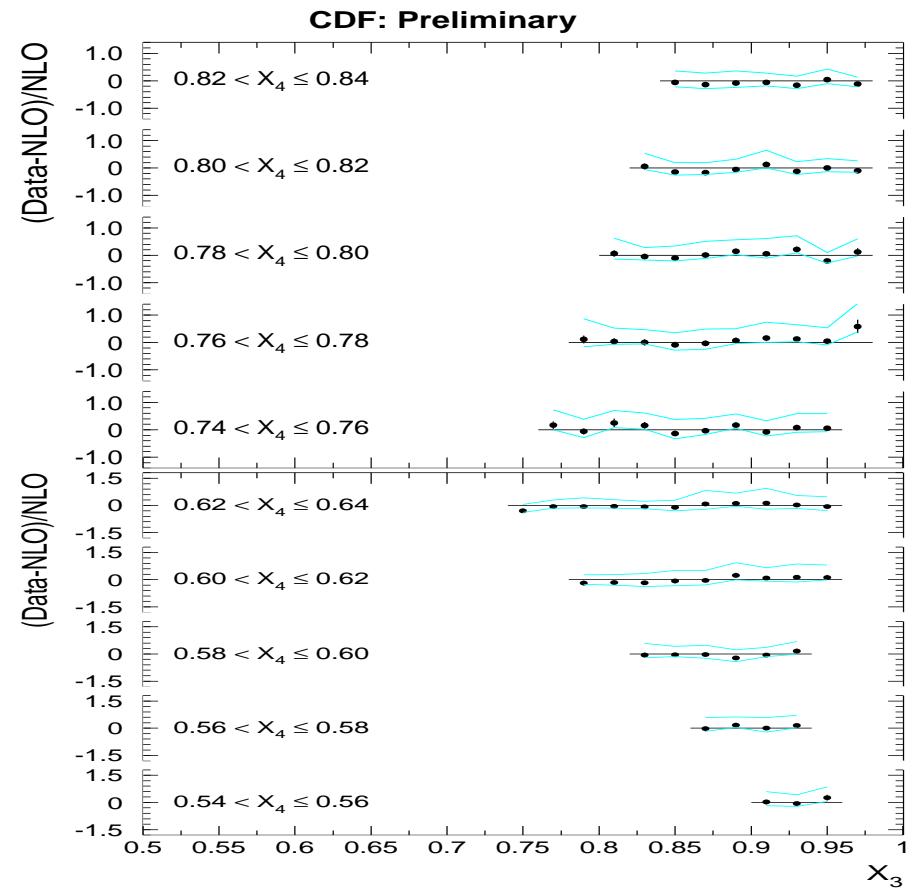
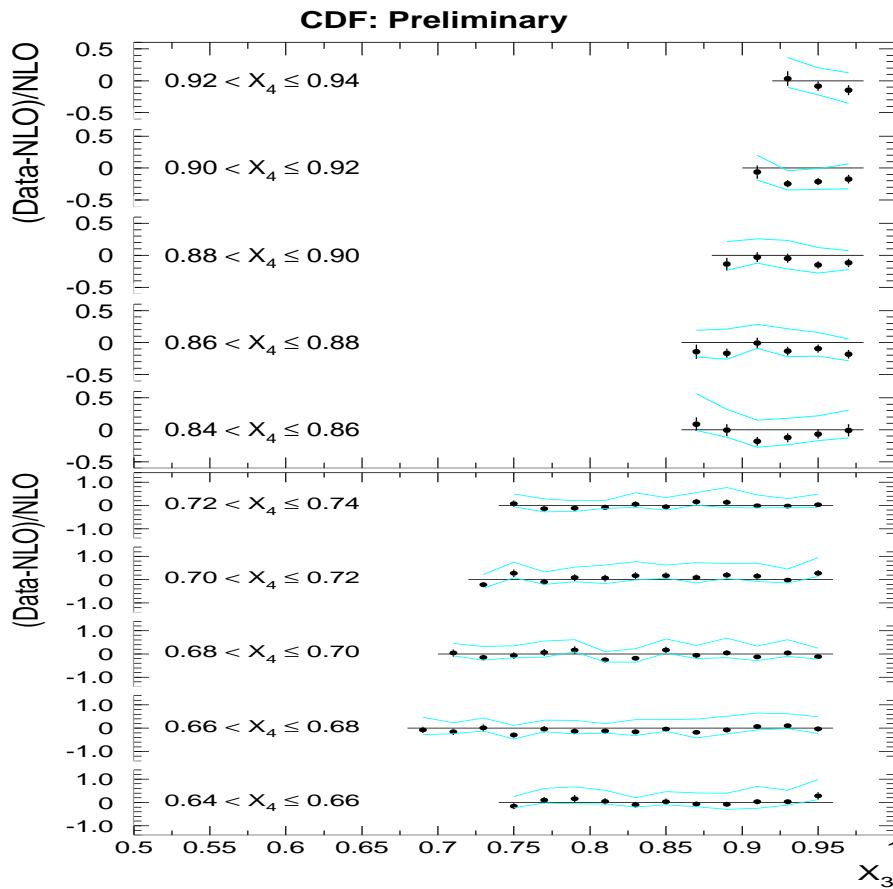
$$X_3 + X_4 + X_5 = 2, \quad X_3 = \frac{2}{3} \dots 1, \quad X_4 = \frac{1}{2} \dots 1, \quad X_5 = 0 \dots \frac{2}{3}.$$

- $\frac{d^2\sigma}{dX_3 dX_4} \propto |\mathcal{M}|^2 \propto \text{density in Dalitz plane.}$



# 3-Jet Production vs. NLO QCD — 1d distributions

- For each bin in  $X_4$ : Plot (Data–NLO)/NLO as a function of  $X_3$ :



- Reasonable agreement within systematic and theoretical uncertainties.
- Dominant source of systematic uncertainty: jet energy scale.
- $\chi^2$  analysis: no sensitivity to  $\alpha_s$
- 3-jet production cross section (integrated over  $X_3 < 0.98$ ):

Data:  $\sigma^{3\text{-jet}} = 456 \pm 2(\text{stat.})^{+202}_{-68} (\text{syst.}) \text{ pb.}$     NLO:  $\sigma^{3\text{-jet}} = 482 \pm 2(\text{stat.})^{+31}_{-72} (\text{theo.}) \text{ pb.}$

# Summary and Outlook

- Inclusive Jet Cross Section (Run II):

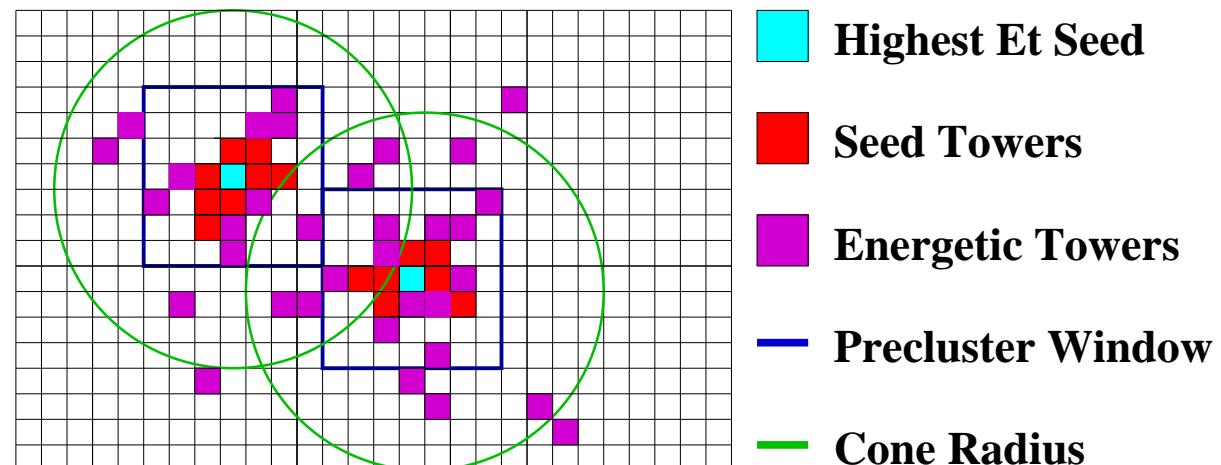
- Run II dataset larger than Run I.
- Measured cross section agrees with prediction from NLO QCD (CTEQ 6.1).
- Ratio  $\sigma^{\text{Run II}}/\sigma^{\text{Run I}}$  agrees with prediction.
- Dominant systematic uncertainty: calorimeter jet energy scale: 5 % (Run I: 1 %).
- Measure jet cross section in forward region. → Sensitivity to high  $x$  gluon.
- Employ Run II jet algorithms: KtClus, MidPoint.

- 3-Jet Production vs. NLO QCD (Run I):

- Reasonable agreement with predictions within systematic and theoretical uncertainties.
- Dalitz analysis: No extraction of  $\alpha_s$  possible.
- Prospects for Run II:
  - higher statistics, reduced systematics, more precise QCD calculations (CPU power)
  - $\alpha_s$  from  $R_{32} = \frac{\sigma^{\text{3-jet}}}{\sigma^{\text{2-jet}}}$  or from event shapes.

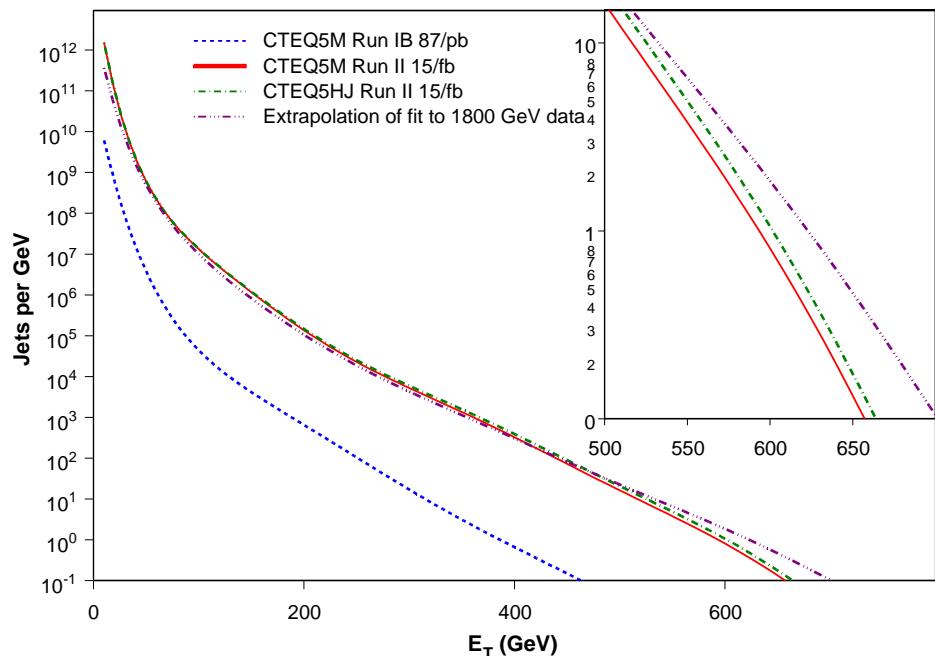
# Backup Slides: JetClu Algorithm

- **JetClu:** CDF's Run I algorithm
  - Create  $E_T$ -ordered list of calorimeter towers (seed towers:  $E_T > 1 \text{ GeV}$ ).
  - Build **pre-clusters** from adjacent seed towers beginning with the highest  $E_T$  tower.
  - For each pre-cluster: Calculate centroid;
    - iterate cone using all towers above 100 MeV
    - $(\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} < R_{\text{cone}})$ .
  - “**Ratcheting**”: During the iteration no seed tower of the original pre-cluster ever leaves the cone! (Pre-clusters remain connected to cones.)
  - Two overlapping stable cones are **merged** if more than 75 % of the transverse energy of one of the cones is shared by the other one.  
Otherwise the cones are **split** by distributing the shared energy among the cones.  
(CDF-specific, iterative)
  - JetClu is neither infrared safe nor collinear safe.
  - Yet, JetClu is being used in CDF's Run II Level 3 trigger and for some analyses (backward compatibility).



# Backup Slides: Central / Forward Region

Jet Yields Bin 1 -  $0.1 < |y| < 0.7$



Jet Yields Bin 4 -  $2.1 < |y| < 3.0$

